

EXTENDS *FiniteSets*, *Sequences*, *Naturals*, *TLC*

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This defines the YARN registry in terms of operations on sets of records.

Every registry entry is represented as a record containing both the path and the data.

It assumes that

1. operations on this set are immediate.
2. selection operations (such as \forall and \exists are atomic)
3. changes are immediately visible to all other users of the registry.
4. This clearly implies that changes are visible in the sequence in which they happen.

A Zookeeper-based registry does not meet all those assumptions

1. changes may take time to propagate across the *ZK* quorum, hence changes cannot be considered immediate from the perspective of other registry clients. (assumptions (1) and (3)).
2. Selection operations may not be atomic. (assumption (2)).

Operations will still happen in the order received by the elected *ZK* master

A stricter definition would try to state that all operations are eventually true excluding other changes happening during a sequence of action. This is left as an exercise for the reader.

CONSTANTS

<i>PathChars</i> ,	the set of valid characters in a path
<i>Paths</i> ,	the set of all possible valid paths
<i>Data</i> ,	the set of all possible sequences of bytes
<i>Address</i> ,	the set of all possible address n-tuples
<i>Addresses</i> ,	the set of all possible address instances
<i>Endpoints</i> ,	the set of all possible <i>endpoints</i>
<i>PersistPolicies</i> ,	the set of persistence policies
<i>ServiceRecords</i> ,	all service records

<i>Registries</i> ,	the set of all possible registries
<i>PutActions</i> ,	all possible put actions
<i>DeleteActions</i> ,	all possible delete actions
<i>PurgeActions</i> ,	all possible purge actions
<i>MkdirActions</i>	all possible <i>mkdir</i> actions

the registry
VARIABLE *registry*

Sequence of actions to apply to the registry
VARIABLE *actions*

Tuple of all variables.

$vars \triangleq \langle registry, actions \rangle$

Persistence policy
 $PersistPolicySet \triangleq \{$
 "MANUAL", persists until manually removed
 "CLUSTER-RESTART", persists until the cluster is restarted
 "APPLICATION", persists until the application finishes
 "APPLICATION-ATTEMPT", persists until the application attempt finishes
 "CONTAINER", persists until the container finishes
 "EPHEMERAL" the record is ephemeral
 $\}$

Type invariants.
 $TypeInvariant \triangleq$
 $\wedge \forall p \in PersistPolicies : p \in PersistPolicySet$

An Entry is defined as a path, an ephemerality flag, and the actual data which it contains.

By including the path in an entry, we avoid having to define some function mapping $Path \rightarrow entry$. Instead a registry can be defined as a set of *RegistryEntries* matching the validity criteria.

$RegistryEntry \triangleq [$
 The path to the entry

$path : Paths,$
 A flag to indicate when the entry is ephemeral
 $ephemeral : \text{BOOLEAN},$
 the data in the entry
 $data : Data$
 $]$

An endpoint in a service record
 $Endpoint \triangleq [$
 API of the endpoint: some identifier
 $api : \text{STRING},$
 A list of address n-tuples
 $addresses : Addresses$
 $]$

A service record
 $ServiceRecord \triangleq [$
 ID – used when applying the persistence policy
 $id : \text{STRING},$
 the persistence policy
 $persistence : PersistPolicySet,$
 A description
 $description : \text{STRING},$
 A set of endpoints
 $external : Endpoints,$
 Endpoints intended for use internally
 $internal : Endpoints$
 $]$

Action Records

$putAction \triangleq [$
 $type : \text{"put"},$
 $record : ServiceRecord$
 $]$
 $deleteAction \triangleq [$
 $type : \text{"delete"},$
 $path : \text{STRING},$

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    recursive : BOOLEAN
]

purgeAction  $\triangleq$  [
    type : "purge",
    path : STRING,
    persistence : PersistPolicySet
]

mkDirAction  $\triangleq$  [
    type : "mkdir",
    path : STRING,
    parents : BOOLEAN
]

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Path operations

parent is defined for non empty sequences

$$\text{parent}(\text{path}) \triangleq \text{SubSeq}(\text{path}, 1, \text{Len}(\text{path}) - 1)$$

$$\text{isParent}(\text{path}, c) \triangleq \text{path} = \text{parent}(c)$$

Registry Access Operations

Lookup all entries in a registry with a matching path

$$\text{lookup}(\text{Registry}, \text{path}) \triangleq \forall \text{entry} \in \text{Registry} : \text{entry.path} = \text{path}$$

A path exists in the registry iff there is an entry with that path

$$\text{exists}(\text{Registry}, \text{path}) \triangleq \text{lookup}(\text{Registry}, \text{path}) \neq \{\}$$

parent entry, or an empty set if there is none

$$\text{parentEntry}(\text{Registry}, \text{path}) \triangleq \text{lookup}(\text{Registry}, \text{parent}(\text{path}))$$

$$\text{isRootPath}(\text{path}) \triangleq \text{path} = \langle \rangle$$

the root entry

$$\text{isRootEntry}(\text{entry}) \triangleq \text{entry.path} = \langle \rangle$$

ephemeral

$$\text{isEphemeral}(\text{entry}) \triangleq \text{entry.ephemeral}$$

A path p is an ancestor of another path d if they are different, and the path d starts with path p

$$\begin{aligned} isAncestorOf(path, d) &\triangleq \\ &\wedge path \neq d \\ &\wedge \exists k : SubSeq(d, 0, k) = path \end{aligned}$$

$$\begin{aligned} ancestorPathOf(path) &\triangleq \\ &\forall a \in Paths : isAncestorOf(a, path) \end{aligned}$$

the set of all children of a path in the registry

$$children(R, path) \triangleq \forall c \in R : isParent(path, c.path)$$

$$\begin{aligned} a \text{ path has children if the } children() \text{ function does not return the empty set} \\ hasChildren(R, path) &\triangleq children(R, path) \neq \{\} \end{aligned}$$

Descendant: a child of a path or a descendant of a child of a path

$$\begin{aligned} descendants(R, path) &\triangleq \forall e \in R : isAncestorOf(path, e.path) \\ ancestors(R, path) &\triangleq \forall e \in R : isAncestorOf(e.path, path) \end{aligned}$$

The set of entries that are a path and its descendants

$$\begin{aligned} pathAndDescendants(R, path) &\triangleq \\ &\vee \forall e \in R : isAncestorOf(path, e.path) \\ &\vee lookup(R, path) \end{aligned}$$

For validity, all entries must match the following criteria

$$\begin{aligned} validRegistry(R) &\triangleq \\ &\text{there can be at most one entry for a path.} \\ &\wedge \forall e \in R : Cardinality(lookup(R, e.path)) = 1 \\ &\text{There's at least one root entry} \\ &\wedge \exists e \in R : isRootEntry(e) \\ &\text{no root entry may be ephemeral} \\ &\wedge \exists e \in R : isRootEntry(e) \Rightarrow \neg e.ephemeral \\ &\text{an entry must be the root entry or have a parent entry} \\ &\wedge \forall e \in R : isRootEntry(e) \vee exists(R, parent(e.path)) \\ &\text{If the entry has data, it must be a service record} \\ &\wedge \forall e \in R : (e.data = \langle \rangle \vee e.data \in ServiceRecords) \\ &\text{if an entry is not root, it cannot have an ephemeral parent} \\ &\wedge \forall e \in R : (isRootEntry(e) \vee \neg isEphemeral(Head(parentEntry(R, e.path)))) \end{aligned}$$

Registry Manipulation

An entry can be put into the registry *iff*

- its parent is present or it is the root *entry*
- if it is marked as ephemeral, there are no child entries in the *registry*
- if it is marked as ephemeral, it is not a change to the root entry

$$\begin{aligned} \text{canPut}(R, e) &\triangleq \\ &\wedge \text{isRootEntry}(e) \vee (\forall p \in \text{parentEntry}(R, e.\text{path}) : \neg p.\text{ephemeral}) \\ &\wedge (\text{isEphemeral}(e) \Rightarrow \neg \text{hasChildren}(R, e.\text{path})) \\ &\wedge (\text{isEphemeral}(e) \Rightarrow \neg \text{isRootEntry}(e)) \end{aligned}$$

put adds/replaces an entry if permitted

$$\begin{aligned} \text{put}(R, e) &\triangleq \\ &\wedge \text{canPut}(R, e) \\ &\wedge R' = (R \setminus \text{lookup}(R, e.\text{path})) \cup e \end{aligned}$$

mkdir() adds a new empty entry where there was none before, *iff*

- the parent *exists*
- it meets the requirement for being “put”

$$\begin{aligned} \text{mkdirSimple}(R, \text{path}) &\triangleq \\ \text{LET } \text{record} &\triangleq [\text{path} \mapsto \text{path}, \text{ephemeral} \mapsto \text{FALSE}, \text{data} \mapsto \langle \rangle] \\ \text{IN } &\vee \text{exists}(R, \text{path}) \\ &\vee (\text{exists}(R, \text{parent}(\text{path})) \wedge \text{canPut}(R, \text{record}) \wedge (R' = R \cup \text{record})) \end{aligned}$$

For all parents, the *mkdirSimple* criteria must apply. This could be defined recursively, except what is not being defined here is a set.

It declares that the *mkdirSimple* state applies to the path and all its parents in the set R'

$$\begin{aligned} \text{mkdirWithParents}(R, \text{path}) &\triangleq \\ &\wedge \forall p2 \in \text{ancestors}(R, \text{path}) : \text{mkdirSimple}(R, p2) \\ &\wedge \text{mkdirSimple}(R, \text{path}) \end{aligned}$$

$$\begin{aligned} \text{mkdir}(R, \text{path}, \text{recursive}) &\triangleq \\ \text{IF } \text{recursive} &\text{ THEN } \text{mkdirWithParents}(R, \text{path}) \text{ ELSE } \text{mkdirSimple}(R, \text{path}) \end{aligned}$$

Deletion is set difference on any existing entries

$$\begin{aligned} \text{simpleDelete}(R, \text{path}) &\triangleq \\ &\wedge \neg \text{isRootPath}(\text{path}) \\ &\wedge \text{children}(R, \text{path}) = \{\} \\ &\wedge R' = R \setminus \text{lookup}(R, \text{path}) \end{aligned}$$

recursive delete: neither the path or its descendants exists in the new registry

TODO: Define the special case of root delete: the path remains but nothing else

$$\begin{aligned} \text{recursiveDelete}(R, \text{path}) &\triangleq \\ &\wedge \neg \text{isRootPath}(\text{path}) \\ &\wedge R' = R \setminus (\text{lookup}(R, \text{path}) \cup \text{descendants}(R, \text{path})) \end{aligned}$$

Delete operation which chooses the recursiveness policy based on an argument

$$\begin{aligned} \text{delete}(R, \text{path}, \text{recursive}) &\triangleq \\ \text{IF } \text{recursive} \text{ THEN } \text{recursiveDelete}(R, \text{path}) \text{ ELSE } \text{simpleDelete}(R, \text{path}) \end{aligned}$$

Purge ensures that all entries under a path with the matching *ID* and policy are not there afterwards

$$\begin{aligned} \text{purge}(R, \text{path}, \text{id}, \text{persistence}) &\triangleq \\ &\wedge (\text{persistence} \in \text{PersistPolicySet}) \\ &\wedge \forall p2 \in \text{pathAndDescendants}(R, \text{path}) : \\ &\quad (p2.\text{id} = \text{id} \wedge p2.\text{persistence} = \text{persistence}) \Rightarrow \text{recursiveDelete}(R, p2.\text{path}) \end{aligned}$$

Resolve() resolves the record at a path or fails

$$\begin{aligned} \text{resolveRecord}(R, \text{path}) &\triangleq \\ \text{LET } l &\triangleq \text{lookup}(R, \text{path}) \text{ IN} \\ &\wedge \text{Cardinality}(l) = 1 \\ &\wedge \text{CHOOSE } e \in l : \text{TRUE} \end{aligned}$$

The specific action of putting an entry into a record includes validating the record

$$\begin{aligned} \text{validRecordToPut}(\text{path}, \text{ephemeral}, \text{record}) &\triangleq \\ &\text{all records declared ephemeral must be put} \\ &\text{as an ephemeral node -and vice versa} \\ &\wedge (\text{ephemeral} \equiv \text{record.persistence} = \text{"EPHEMERAL"}) \end{aligned}$$

The root entry must have manual persistence

$$\wedge (\text{isRootPath}(\text{path}) \Rightarrow \text{record.persistence} = \text{"MANUAL"})$$

putting a service record involves validating it then putting it in the registry marshalled as the data in the entry

$$\begin{aligned} \text{putRecord}(R, \text{path}, \text{ephemeral}, \text{record}) &\triangleq \\ &\wedge \text{validRecordToPut}(\text{path}, \text{ephemeral}, \text{record}) \\ &\wedge \text{put}(R, [\text{path} \mapsto \text{path}, \text{ephemeral} \mapsto \text{ephemeral}, \text{data} \mapsto \text{record}]) \end{aligned}$$

The action queue can only contain one of the sets of action types, and by giving each a unique name, those sets are guaranteed to be disjoint

$$\begin{aligned}
\text{QueueInvariant} &\triangleq \\
&\wedge \forall a \in \text{actions} : \\
&\quad \vee (a \in \text{PutActions} \wedge a.\text{type} = \text{"put"}) \\
&\quad \vee (a \in \text{DeleteActions} \wedge a.\text{type} = \text{"delete"}) \\
&\quad \vee (a \in \text{PurgeActions} \wedge a.\text{type} = \text{"purge"}) \\
&\quad \vee (a \in \text{MkdirActions} \wedge a.\text{type} = \text{"mkdir"})
\end{aligned}$$

Applying queued actions

$$\begin{aligned}
\text{applyAction}(R, a) &\triangleq \\
&\vee (a \in \text{PutActions} \wedge \text{putRecord}(R, a.\text{path}, a.\text{ephemeral}, a.\text{record})) \\
&\vee (a \in \text{MkdirActions} \wedge \text{mkdir}(R, a.\text{path}, a.\text{recursive})) \\
&\vee (a \in \text{DeleteActions} \wedge \text{delete}(R, a.\text{path}, a.\text{recursive})) \\
&\vee (a \in \text{PurgeActions} \wedge \text{purge}(R, a.\text{path}, a.\text{id}, a.\text{persistence}))
\end{aligned}$$

Apply the first action in a list and then update the actions

$$\begin{aligned}
\text{applyFirstAction}(R, a) &\triangleq \\
&\wedge \text{actions} \neq \langle \rangle \\
&\wedge \text{applyAction}(R, \text{Head}(a)) \\
&\wedge \text{actions}' = \text{Tail}(a)
\end{aligned}$$

$$\text{Next} \triangleq \text{applyFirstAction}(\text{registry}, \text{actions})$$

All submitted actions must eventually be applied.

$$\text{Liveness} \triangleq \Diamond(\text{actions} = \langle \rangle)$$

The initial state of a registry has the root entry.

$$\begin{aligned}
\text{InitialRegistry} &\triangleq \text{registry} = \{ \\
&\quad [\text{path} \mapsto \langle \rangle, \text{ephemeral} \mapsto \text{FALSE}, \text{data} \mapsto \langle \rangle] \\
&\}
\end{aligned}$$

The valid state of the “registry” variable is defined as Via the *validRegistry* predicate

$$\text{ValidRegistryState} \triangleq \text{validRegistry}(\text{registry})$$

The initial state of the system

$$\begin{aligned}
\text{InitialState} &\triangleq \\
&\wedge \text{InitialRegistry} \\
&\wedge \text{ValidRegistryState} \\
&\wedge \text{actions} = \langle \rangle
\end{aligned}$$

The registry has an initial state, the series of state changes driven by the actions, and the requirement that it does act on those actions.

$$\begin{aligned} RegistrySpec &\triangleq \\ &\wedge InitialState \\ &\wedge \Box [Next]_{vars} \\ &\wedge Liveness \end{aligned}$$

Theorem: For all operations from that initial state, the registry state is still valid

THEOREM $InitialState \Rightarrow \Box ValidRegistryState$

Theorem: for all operations from that initial state, the type invariants hold

THEOREM $InitialState \Rightarrow \Box TypeInvariant$

THEOREM $InitialState \Rightarrow \Box QueueInvariant$
